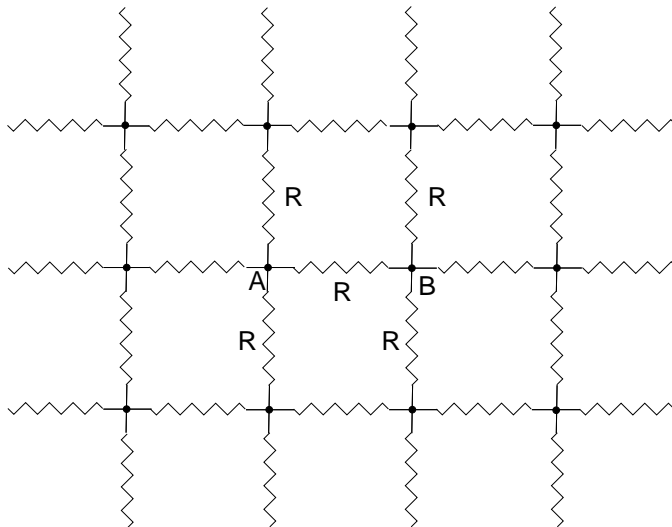


An infinite number of identical resistors are connected in a square grid as shown. What is the effective resistance between two neighboring junctions (i.e. between  $A$  and  $B$ ).



If current  $+I_0$  is injected at point  $A$  and allowed to flow to infinity, each of the resistors connected directly to point  $A$  will, by symmetry, carry  $I_0/4$  directed away from  $A$ . Similarly, if current  $-I_0$  is injected at point  $B$ , each resistor connected to  $B$  will carry current  $I_0/4$  directed toward  $B$ . Superposing these two solutions yields a solution where current is injected at  $A$  and extracted at  $B$ . The net current flowing along the resistor connecting them is  $I_0/2$  and so the voltage drop between  $A$  and  $B$  is  $V = I_0 R/2$ . **The effective resistance of the network is therefore  $V/I_0 = R/2$ .**